

Exponent Rules 1 to 4

Definitions:	A coefficient is a regular number (usually a whole number) which multiplies some variable. A base is a regular number (usually a whole number) which can be raised to another power. An exponent is the super-scripted value which notes how many times a base is multiplied by itself. Expanded notation uses the none-exponent version of numbers to show or check the simplified value of bases and exponents.
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Formulas:	Rule #1 $(x^a)(x^b) = x^{a+b}$	Rule #2 $(x^a)^b = x^{ab}$	Rule #3 $(xyz)^a = x^a y^a z^a$	Rule #4 $(n)^0 = 1 / 1 = 1$
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Example #1 ...using rule #1	$(x^4) \cdot (x^3) = \cancel{x^4}^{4+3} = \cancel{x^7}$ $\cancel{xxxx} \cdot \cancel{xxx}$	$(3x^4) \cdot (5x^3) = \cancel{3} \cancel{5} x^{4+3} = \cancel{15} x^7$ $\cancel{3xxx} \cdot \cancel{5xxx}$	$2(3x^4) \cdot (5x^3) = \cancel{2} \cdot \cancel{15} x^7 = \cancel{30} x^7$
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Example #2 ...using rule #1	$(x^6) \cdot (x^8) = \cancel{x^6}^{6+8} = \cancel{x^{14}}$ $\cancel{xxxxxx} \cdot \cancel{xxxxxxxx}$	$(-x^6) \cdot (4x^8) = -1 \cdot 4 x^{6+8} = -4 x^{14}$ $\cancel{-xxxxxx} \cdot \cancel{4xxxxxxxx}$	$7(-x^6) \cdot (4x^8) = -4 x^{14} \cdot 7 = -28 x^{14}$
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$(x^a)(x^b) =$ we use either the exponent rule #1 or x^{a+b} the expanded notation to solve each. The expanded notation shows why the rule works.

Example #3 ...using rule #2	$(x^4)^3 = \cancel{x^4}^{4 \cdot 3} = \cancel{x^{12}}$ $\cancel{xxxx} \cdot \cancel{xxxx} \cdot \cancel{xxxx}$	$(5x^4)^3 = \cancel{5}^3 x^{4 \cdot 3} = \cancel{125} x^{12}$ $\cancel{5xxxx} \cdot \cancel{5xxxx} \cdot \cancel{5xxxx}$	$2(5x^4)^3 = \cancel{2} \cdot \cancel{125} x^{12} = \cancel{250} x^{12}$ $\cancel{2 \cdot 5xxxx} \cdot \cancel{5xxxx} \cdot \cancel{5xxxx}$
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Example #4 ...using rule #2	$(x^5)^2 = \cancel{x^5}^{5 \cdot 2} = \cancel{x^{10}}$ $\cancel{xxxxx} \cdot \cancel{xxxxx}$	$(4x^5)^2 = \cancel{4}^2 x^{5 \cdot 2} = \cancel{16} x^{10}$ $\cancel{4xxxxx} \cdot \cancel{4xxxxx}$	$7(4x^5)^2 = \cancel{7} \cdot \cancel{4}^2 x^{5 \cdot 2} = \cancel{112} x^{10}$ $\cancel{7 \cdot 4xxxxx} \cdot \cancel{4xxxxx}$
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$(x^a)^b =$ Exponent Rule 2 tells us to raise an exponent to an exponent by multiplying. The expanded notation shows us why it works.

Example #5 ...using rule #3	$(xyz)^4 = \cancel{x^4}y^4z^4$ $\cancel{x^4}y^4z^4$ $xyz \cdot xyz \cdot xyz \cdot xyz$	$(3xyz)^4 = \cancel{3^4}x^4y^4z^4$ $\cancel{3^4}x^4y^4z^4$ $3xyz \cdot 3xyz \cdot 3xyz \cdot 3xyz$	$5(3xyz)^4 = \cancel{5 \cdot 3^4}x^4y^4z^4$ $\cancel{5 \cdot 3^4}x^4y^4z^4$ $5 \cdot 3xyz \cdot 3xyz \cdot 3xyz \cdot 3xyz$
Example #6 ...using rule #3	$(wxyz)^2 = \cancel{w^2}x^2y^2z^2$ $\cancel{w^2}x^2y^2z^2$ $wxyz \cdot wxyz$	$(8wxyz)^2 = \cancel{8^2}w^2x^2y^2z^2$ $\cancel{8^2}w^2x^2y^2z^2$ $8 \cdot wxyz \cdot 8wxyz$	$-3(8wxyz)^2 = \cancel{-3 \cdot 8^2}w^2x^2y^2z^2$ $\cancel{-3 \cdot 8^2}w^2x^2y^2z^2$ $-3 \cdot 8wxyz \cdot 8wxyz$

$$(xyz)^a = x^a y^a z^a$$

In each case, using rule #3, we see the exponent effect every part of the expression... in the parentheses. Expanding notation helps us see why.

Example #7 ...using rule #4	$(x)^0 = \frac{x}{x} = 1$ $\frac{x}{x} = 1$	$(5x)^0 = \frac{5x}{5x} = 1$ $\frac{5x}{5x} = 1$	$3(5x)^0 = 3 \cdot \frac{5x}{5x} = 3$ $3 \cdot \frac{5x}{5x} = 3$
Example #8 ...using rule #4	$(x^3y^0)^2 = (\cancel{x^3} \cdot 1)^2 =$ $\cancel{x^3}$ $xxx \cdot xxx$	$(2x^3y^0)^2 = (2\cancel{x^3} \cdot 1)^2 =$ $2\cancel{x^3}$ $2xxx \cdot 2xxx$	$4(2x^3y^0)^2 = 4 \cdot (2x^3 \cdot 1)^2 =$ $16x^6$ $4 \cdot 2xxx \cdot 2xxx$

$$n^0 = \frac{n}{n} = 1$$

We know all numbers to the zero-power equal "1." Example 7's expanded notation shows us why. Example #8 shows us why a zero-exponent does not make all answers a one if something else is multiplying.